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B+ Trees

Today: Chapters 10.1 - 10.5

Motivation

Some applications require two views of a file:

Indexed view:	Sequential view:	
Records are indexed	Records can be sequentially	
by a key accessed in order by ke		
Direct, indexed access Sequential access (pl		
	cally contiguous records)	
Interactive, random	Batch processing (Ex: co-	
access	sequential processing)	

Example of applications

- Student record system in a university:
 - Indexed view: access to individual records
 - Sequential view : batch processing when posting grades or when fees are paid
- Credit card system:
 - Indexed view: interactive check of accounts
 - Sequential view: batch processing of payment slips

We will look at the following two aspects of the problem:

- 1. Maintaining a **sequence set**: keeping records in sequential order
- 2. Adding an **index set** to the sequence set

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Maintaining a Sequence Set

Sorting and re-organizing after insertions and deletions is out of question. We organize the sequence set in teh following way:

- Records are grouped in **blocks**
- Blocks should be at least half full.
- Link fields are used to point to the preceding block and the following block (similarly to doubly linked lists)
- Changes (insertion/deletion) are localized into blocks by performing:
 - Block Splitting when insertion causes overflow
 - Block Merging or Redistribution when deletion causes underflow

Example:

Block size = 4

key: Last Name

Forward Pointer

--- **→** Backward Pointer

• Insertion with overflow:

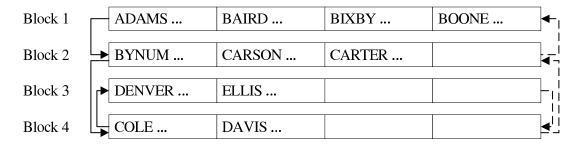
DIOCK I ADAMS DIAD I CARSOI COLL	Block 1	ADAMS	BIXBY	CARSON	COLE
----------------------------------	---------	-------	-------	--------	------

Insert "BAIRD ..."

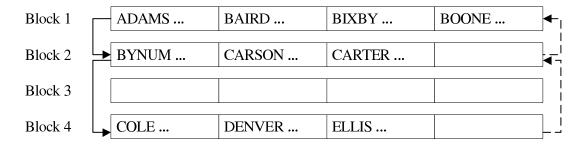


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• Deletion with merging:



Delete "DAVIS ..." (Merging)



Block 3 is available for re-use

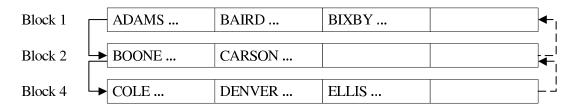
Delete 'BYNUM':

Just remove it from Block 2

Then, delete 'CARTER':

We can either merge Block 2 and 4 or redistribute records among Blocks 1 and 2.

• Deletion with redistribution:



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When previous and next blocks are full then redistribution is the only option.

Advantages and disadvantages of the scheme described

Advantages:

- No need to re-organize the whole file after insertions/deletions.

Disadvantages:

- File takes more space than unblocked files (since blocks may be half full).
- The order of the records is not necessarily **physically** sequential (we only guarantee physical sequentiality within a block).

Choosing Block Size

Consider:

- Main memory constraints (must hold at least 2 blocks)
- Avoid seeking within a block (Ex: in sector formatted disks choose block size equal to cluster size).

Adding an Index Set to the Sequential Set

Index Containing Separators Instead of Keys

Choose the **Shortest Separator** (a prefix)

Block	Range o	of Keys	Separator
1	ADAMS -	BERNE	
2	BOLEN -	CACE	B0
2	DOLEM -	CAGE	CAM
3	CAMP -	- DUTTON	T.
4	EMBRY -	· EVANS	E
_		FOT 17	F
5	FABER -	· FULK	FOLKS
6	FOLKS -	- GADDIS	

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To find a separator for key1= "CAGE" and key2 = "CAMP" find the smallest prefix of key2 that is not a prefix of key1, which is "CAM" in this example.

The Simple Prefix B+ Tree

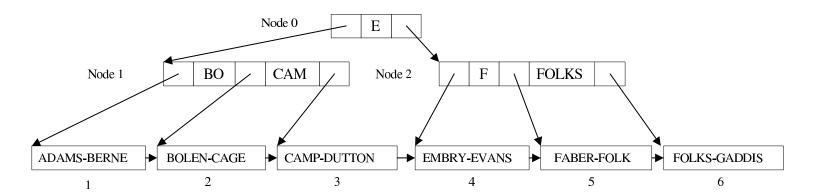
The simple prefix B+ tree consists of:

- the **sequence set** (as seen previously).
- the **index set**: similar to a B-tree index, but storing the shortest separators (prefixes) for the sequence set.

Note: If a node contains N separators, it will contain N+1 children. The fact that we are dealing with separators slightly modifies the operations in the B-tree index.

Example:

Order of the index set is 3 (i.e. maximum of 2 separators and 3 children). Note: The order is usually much larger, but we made it small for this example.



Search in a simple prefix B+ tree: Search for "EMBRY":

- Retrieve Node 0 (root).
- "EMBRY" > "E", so go right, and retrieve Node2.
- Since "EMBRY" < "F" go left, and retrieve block number 4.
- Look for the record with key "EMBRY" in block number 4.